

Fluctuations in the aging dynamics of structural glasses

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Motivation

- Experiments show spatially heterogeneous dynamics.
- Goal: understanding spatial fluctuations in glassy dynamics.

Outline

1. Experiments show strong fluctuations (“dynamic heterogeneities”) in the aging regime.
2. Soft mode approach to local fluctuations: the age of the sample fluctuates locally. Scaling predictions and simulation results for local fluctuations in a spin glass.
3. Scaling in the behavior of local fluctuations in a structural glass: probability distributions of one-point, two-time observables.
4. Scaling in the behavior of local fluctuations in a structural glass: spatial correlations.
5. Scaling in the behavior of local fluctuations in a structural glass: crossover between aging and equilibrium regimes.

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The Problem: Dynamical heterogeneities

Colloid: confocal microscopy (Courtland and Weeks, J. Phys. Cond. Mat **15** S359 (2003))

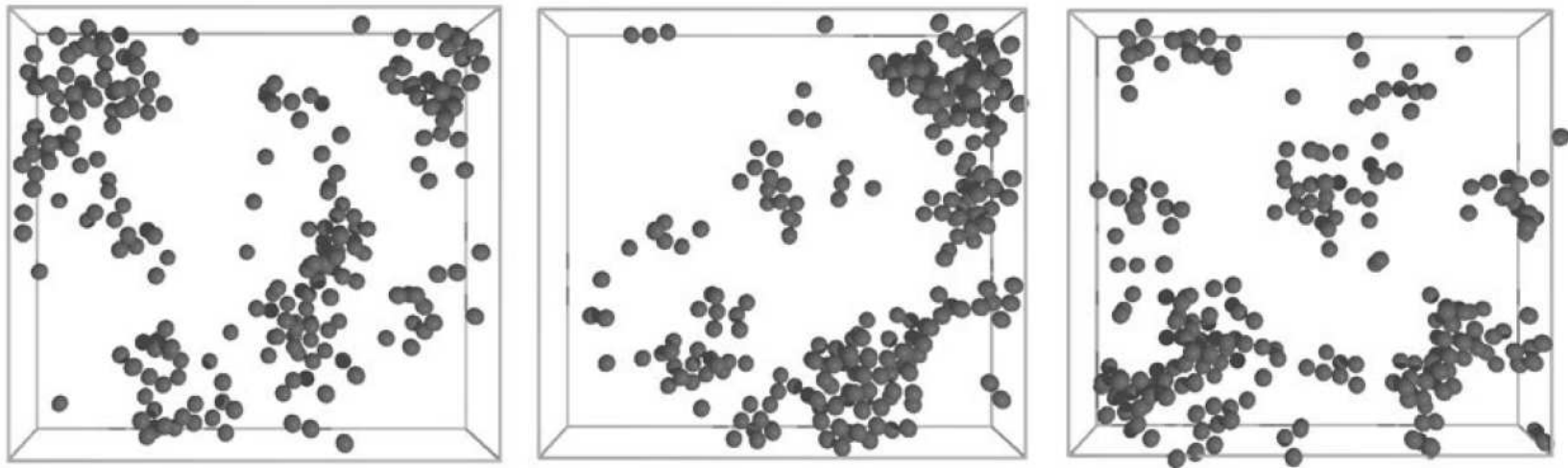
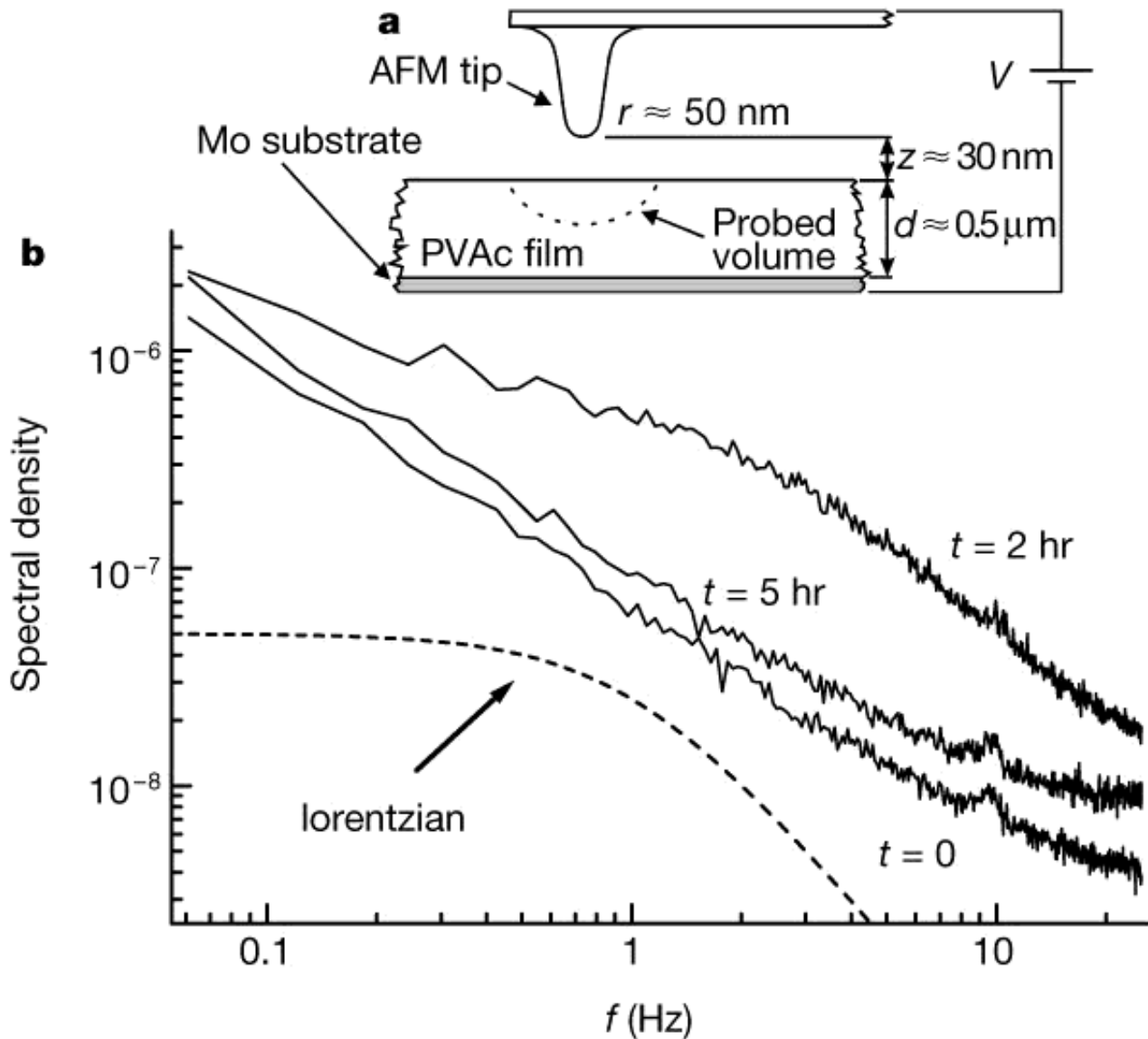


Figure 4. Locations of the 10% most mobile particles at three different ages t_w . For each picture, mobility was determined by calculating displacements Δr over an interval $[t_w, t_w + \Delta T]$, with $\Delta T = 10$ min. Left: $t_w = 10$ min, and $\Delta r > 0.43 \mu\text{m}$ for the most mobile particles. Middle: $t_w = 55$ min, $\Delta r > 0.34 \mu\text{m}$. Right: $t_w = 95$ min, $\Delta r > 0.33 \mu\text{m}$. The data are the same as shown in previous figures, and the choices of t_w correspond to local maxima of γ in figure 2(a). The particles are drawn to scale ($2.36 \mu\text{m}$ diameter) and the box shown is the entire viewing volume (within a much larger sample chamber).

The Problem: Dynamical heterogeneities

PVAc: dielectric fluctuations (Vidal Russell & Israeloff, Nature **408**, 695 (2000))



Polymer glass,
 $T = T_g - 9K$,
transient
appearance of
strongly
fluctuating
region under tip

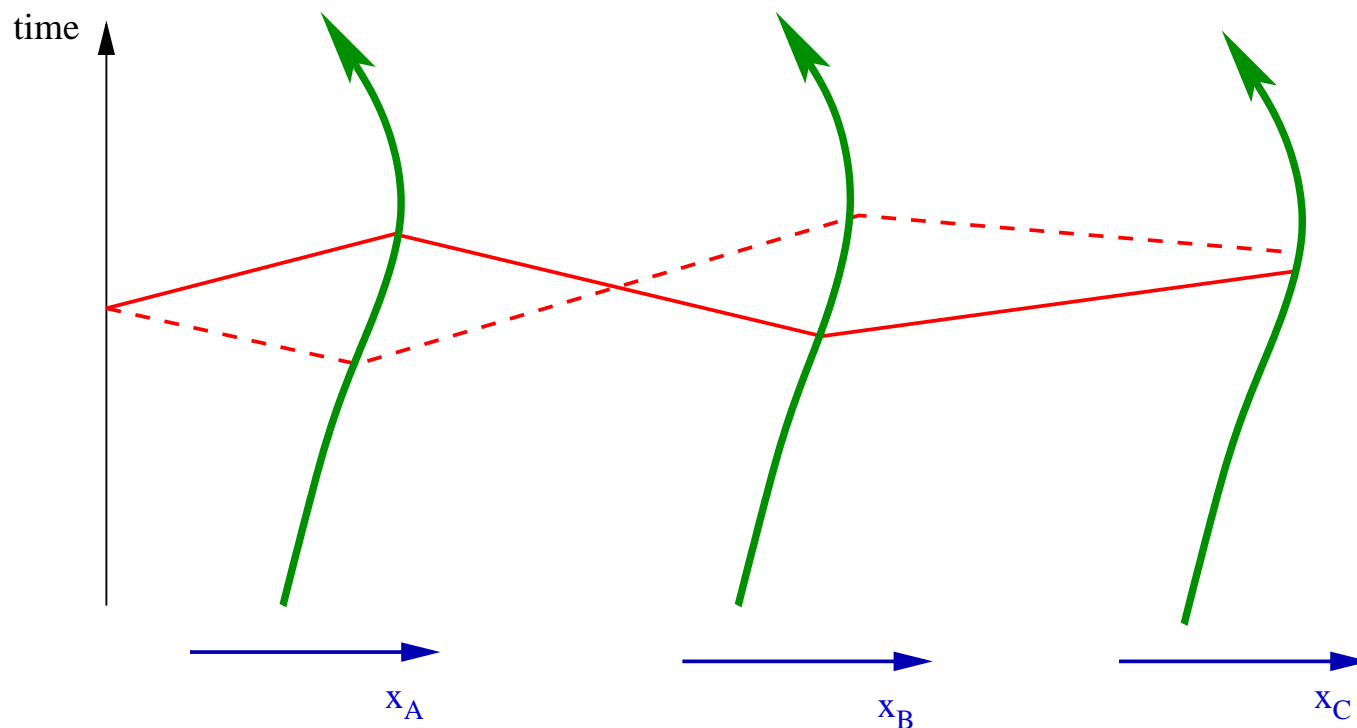
Heterogeneity
lifetime \approx
relaxation time

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Can we understand dynamical heterogeneities in aging systems?

A possible explanation: the glassy material is aging, but the ages are fluctuating in space.



RG in time: reparametrizations $t \rightarrow h(t)$ leave “dynamical action” \mathcal{S} unchanged (irrelevant terms break symmetry at finite times) (C.Chamon, M.P.Kennett, H.E.C., L.F.Cugliandolo, PRL **89**, 217201 (2002))

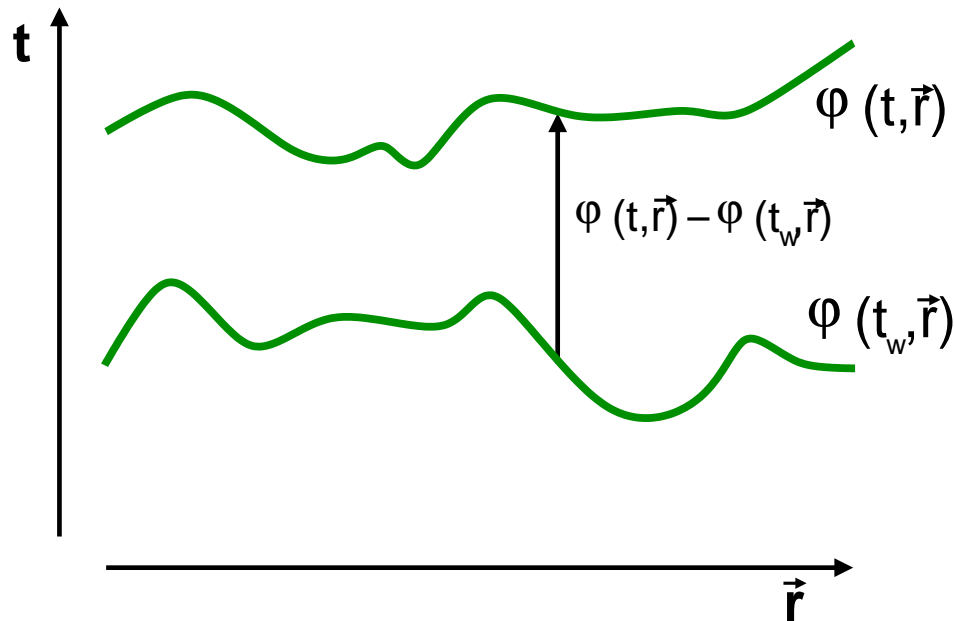
Probability distribution of local correlations: $\rho(C_{\vec{r}})$

(with C. Chamon, L. Cugliandolo, J. Iguain, and M. Kennett: PRL **88**, 237201 (2002) and PRB **68**, 134442 (2003))

If $C_0(t, t_w) \approx C_0(h(t)/h(t_w))$ (for example, $h(t) \approx t$ in 3DEA) then:

$$t \rightarrow h_{\vec{r}}(t) = e^{\varphi_{\vec{r}}(t)}$$

$$C_{\vec{r}}(t, t_w) = C_0(h_{\vec{r}}(t)/h_{\vec{r}}(t_w)) = C_0(\exp(\varphi_{\vec{r}}(t) - \varphi_{\vec{r}}(t_w)))$$



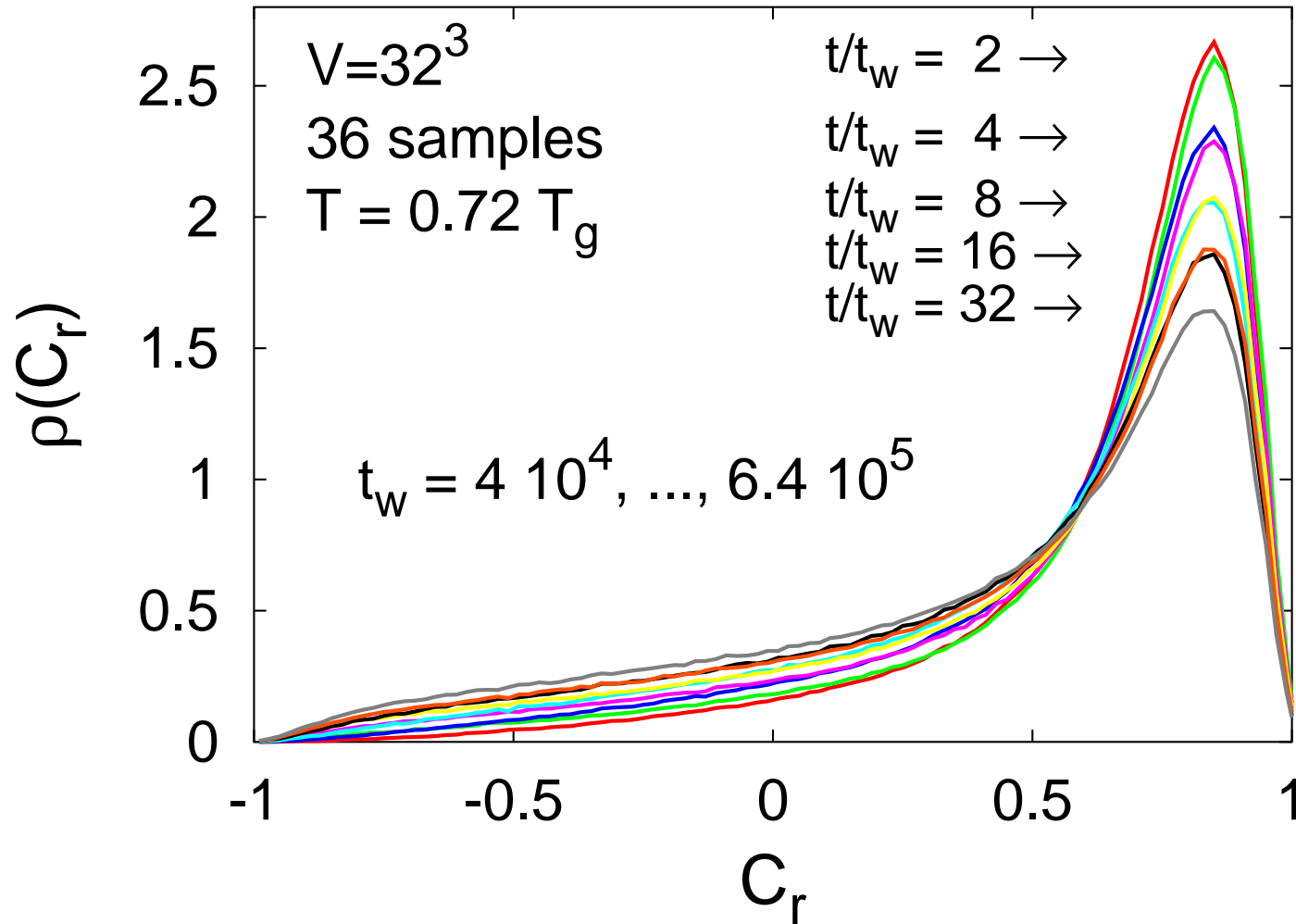
- Fluctuating $\varphi_{\vec{r}}(t)$

- Time reparametrization invariance

- $\Rightarrow \varphi_{\vec{r}}(t) - \varphi_{\vec{r}}(t_w) \approx$

$$\ln\left(\frac{h(t)}{h(t_w)}\right) + \sqrt{a + b \ln\left(\frac{h(t)}{h(t_w)}\right)} X_r$$

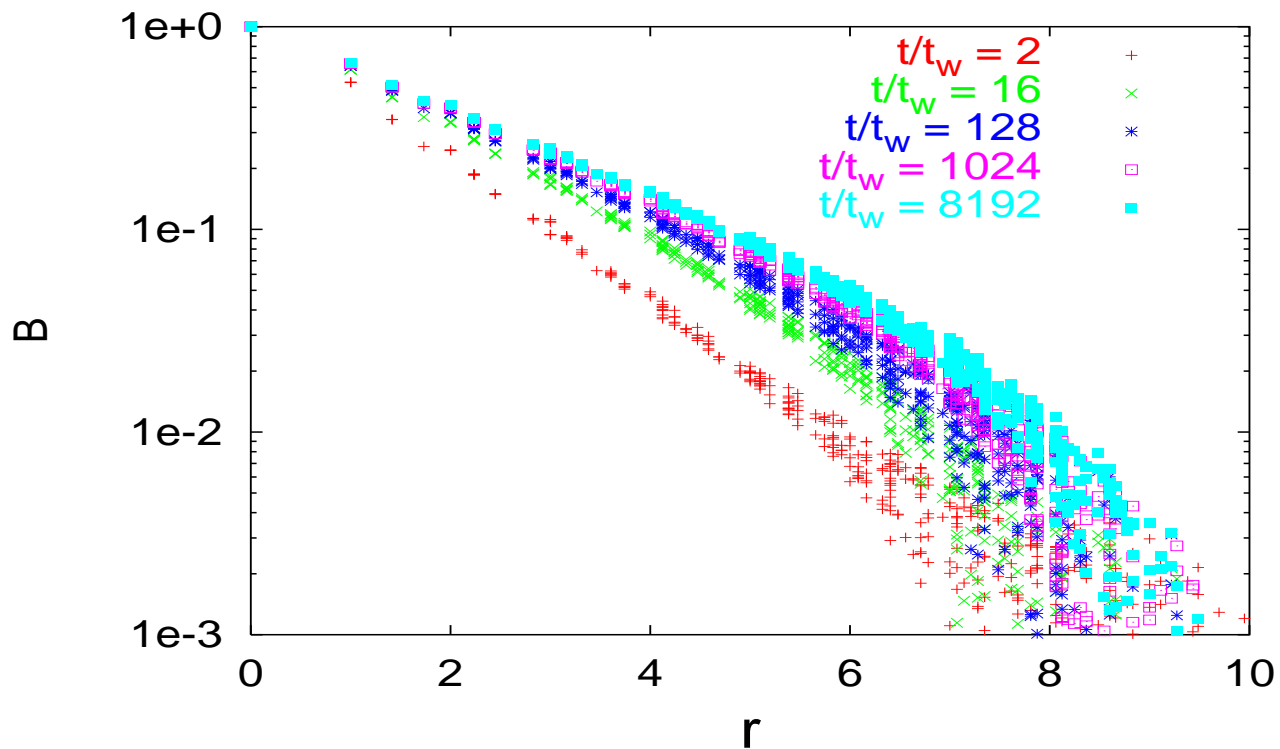
Collapse of $\rho(C_{\vec{r}})$ for fixed t/t_w



Noise-noise spatial correlations: exponential decay

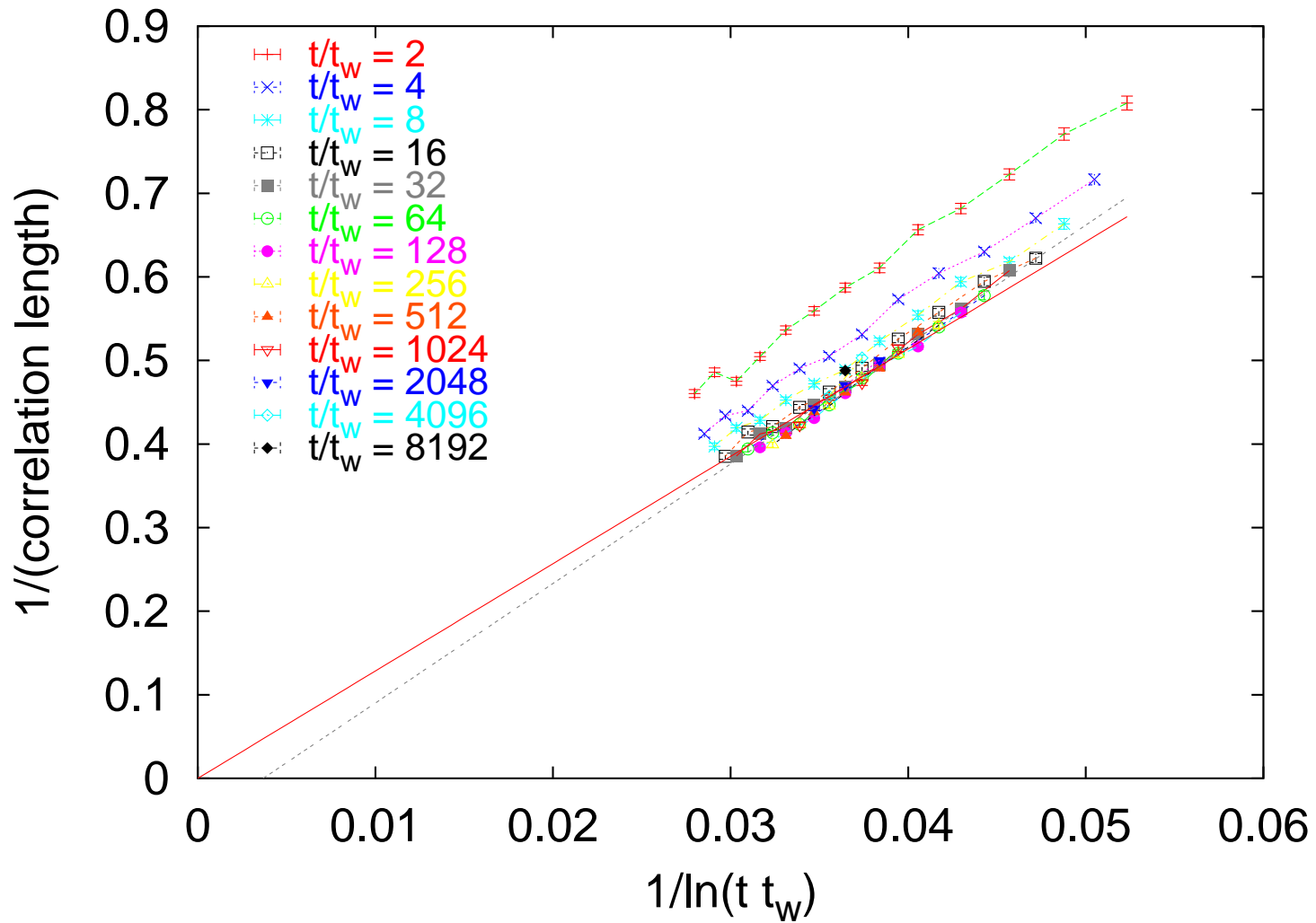
RG-irrelevant \Rightarrow expect finite correlation length
symmetry-breaking terms $(\rightarrow \infty$ for infinite t, t_w).

$$B(\vec{r}, t, t_w) \equiv \langle \delta C_{\vec{r}_i}(t, t_w) \delta C_{\vec{r}_i + \vec{r}}(t, t_w) \rangle_{\vec{r}_i}$$



$t_w = 10^4$ MCs, $V = 32^3$, $T = 0.72T_g$, 64 disorder realizations

Correlation length $\xi(t, t_w) \rightarrow \xi(tt_w)$



$V = 32^3$, $T = 0.72T_g$, 64 disorder realizations

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Structural glass simulations

- 80:20 binary Lennard-Jones mixture, 8000 particles. Thermalized at $T_i = 5.0$, time origin at instantaneous quench to $T_f = 0.4$ (below $T_g \approx 0.435$). Evolves for up to 100000 LJ units (i.e. $\sim 10^{-8}s$) after quench. β relaxation time is of the order of 1 LJ unit. Repeated for 250 to 4000 independent runs (depending on timescale).
- Divide the system in regions, and measure one point, two time quantities for each region.

$$C_{\vec{r}}^{\text{part}}(t, t_w) \equiv \frac{1}{\mathcal{N}(V_{\vec{r}})} \sum_{\vec{r}_i(t_w) \in V_{\vec{r}}} \cos(\vec{q} \cdot [\vec{r}_i(t) - \vec{r}_i(t_w)])$$

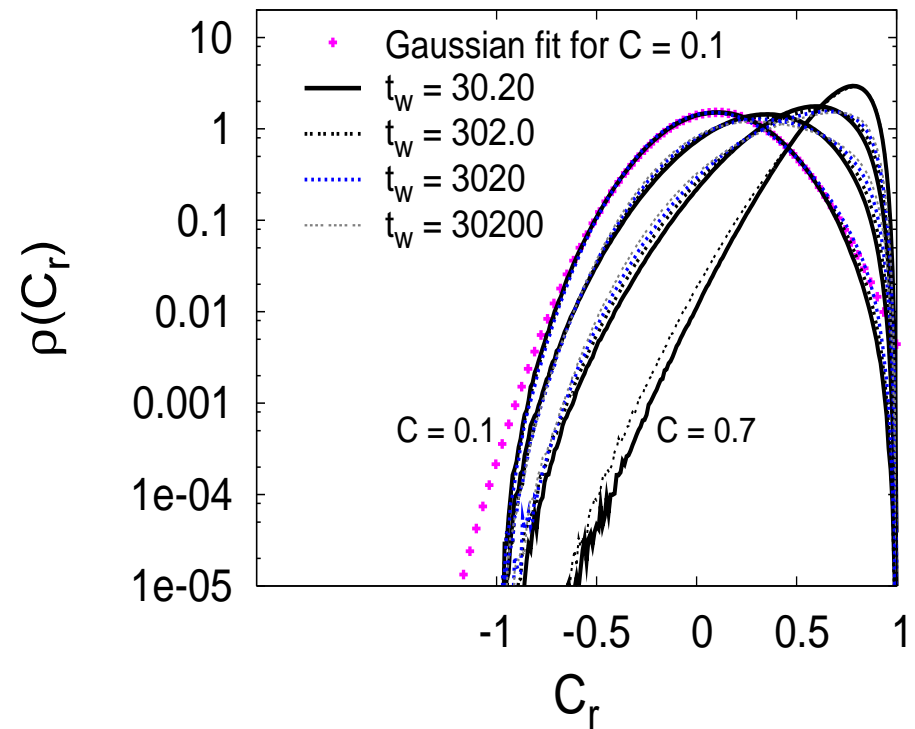
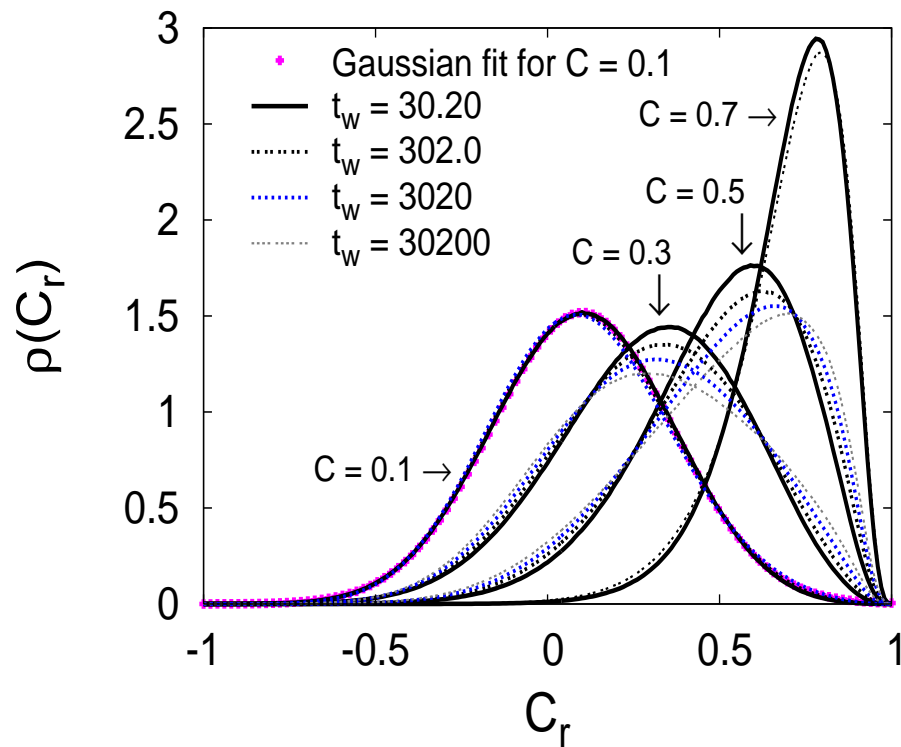
Obtain the probability distributions $\rho(C_r)$ for the local values.

- Use the *global* intermediate scattering function

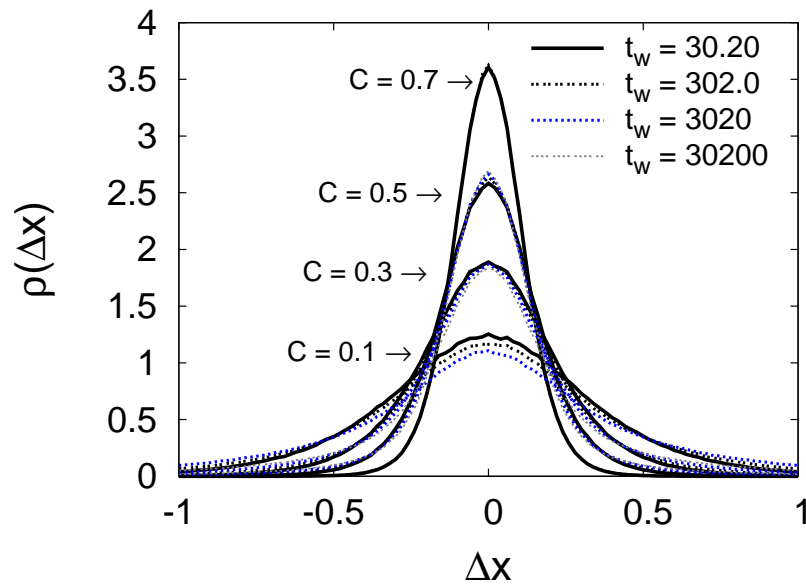
$$C_{\text{global}}(t, t_w) \equiv \frac{1}{N} \sum_{i=1}^N \cos(\vec{q} \cdot [\vec{r}_i(t) - \vec{r}_i(t_w)])$$

to quantify how correlated the system is between times t_w and t .

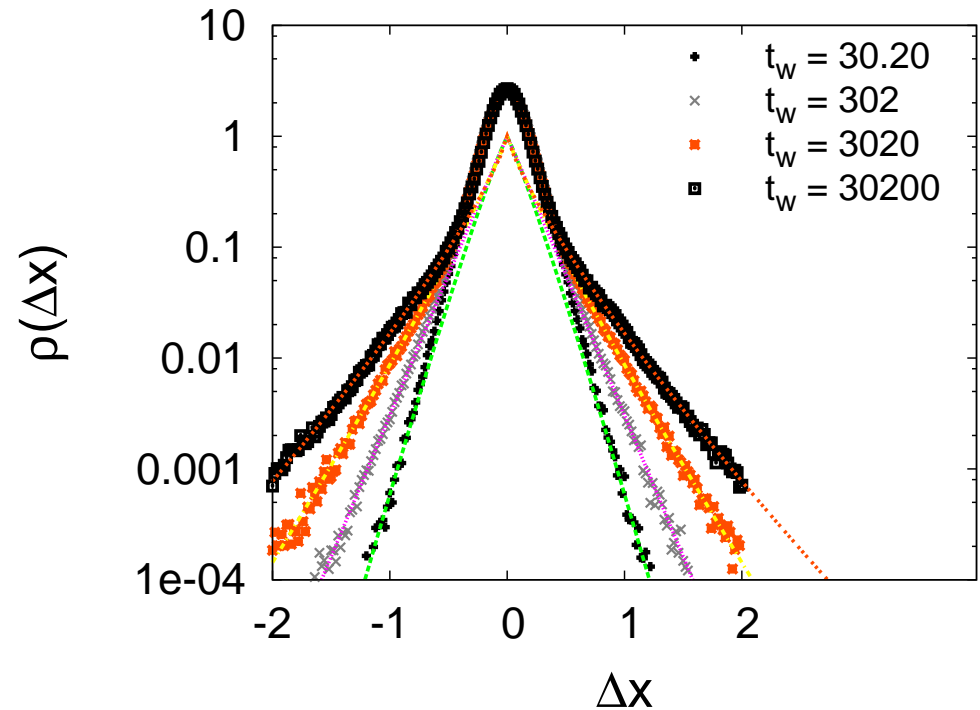
Approximate collapse of $\rho(C_r)$ at constant $C_{\text{global}}(t, t_w)$



Distribution of one-dimensional displacements $\rho(\Delta x)$

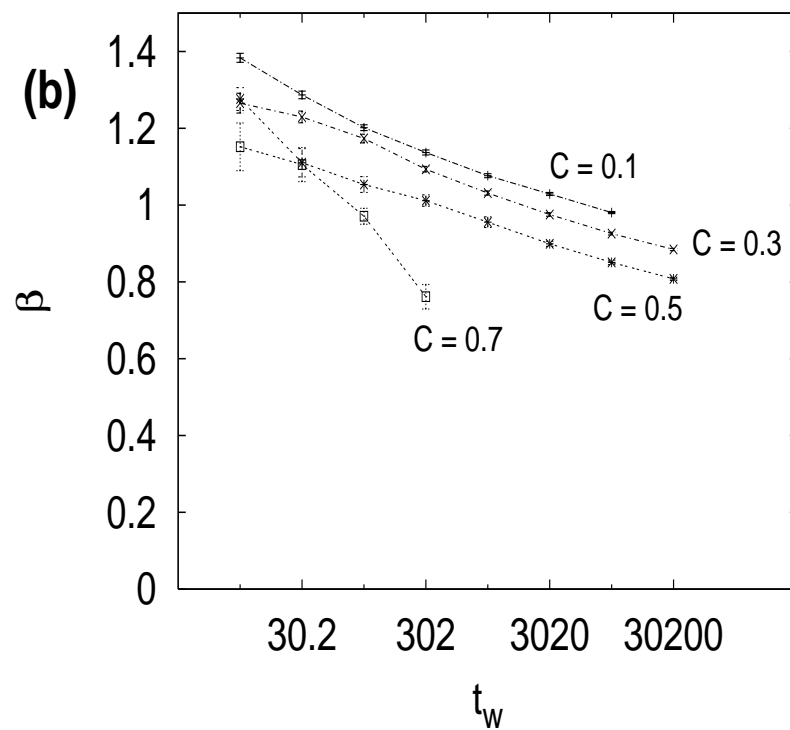
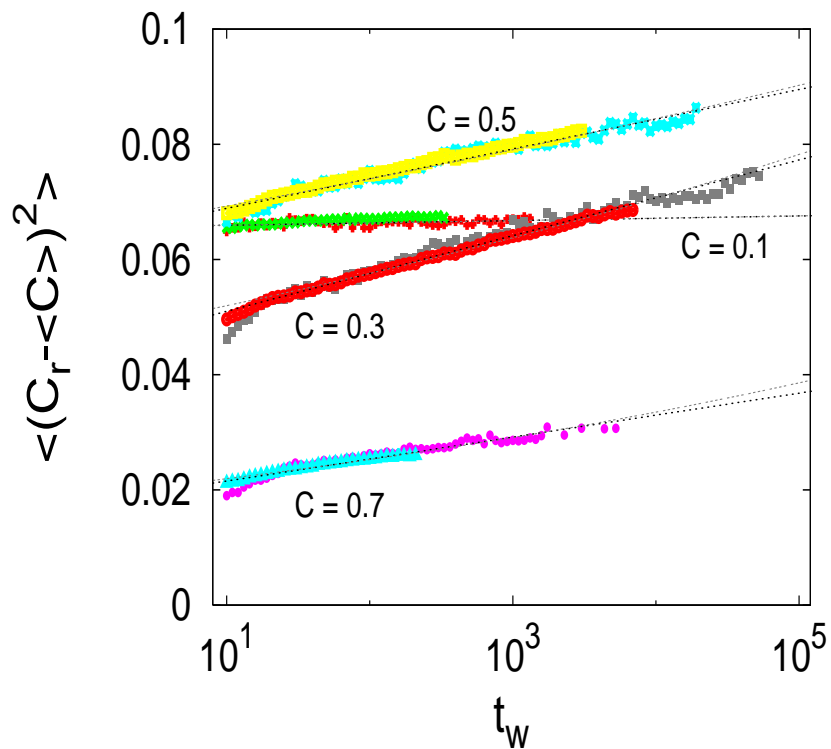


approximate collapse at
constant $C_{\text{global}}(t, t_w)$.



nonlinear exponential tails
 β exponent decreases for
increasing t_w

Slow t_w dependences at constant $C_{\text{global}}(t, t_w)$



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Dynamical correlations: densities

(Lačević, Starr, Schrøder, Glotzer J. Chem. Phys **119**, 7372 (2003))

$$\begin{aligned}w(\mathbf{r}, t, t_w) &= 1 \text{ if particle at } \mathbf{r} \text{ has moved } < a_{\text{vib}} \\ &= 0 \text{ otherwise}\end{aligned}$$

$$g_4(\mathbf{r}, t, t_w) = \text{spatial correlation of } w(\mathbf{r}, t, t_w)$$

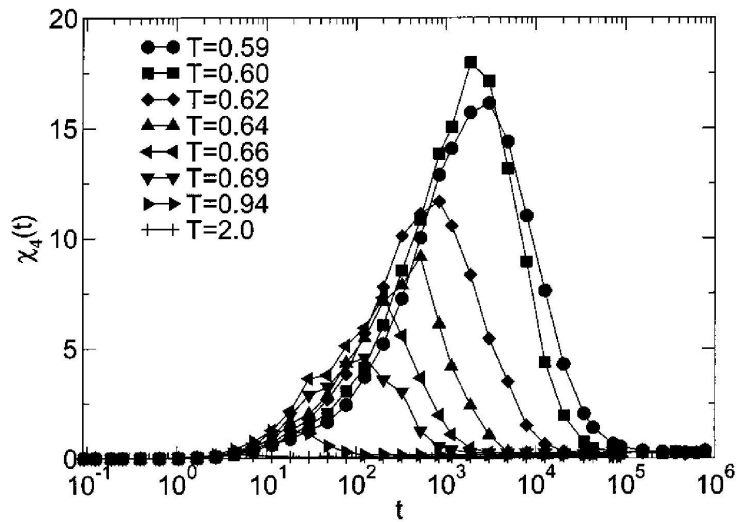
$$\xi_4(t, t_w) = \text{correlation length for } g_4(\mathbf{r}, t, t_w)$$

$$\begin{aligned}\chi_4(t, t_w) &= \text{dynamic density susceptibility} \\ &\propto \int d^3r g_4(\mathbf{r}, t, t_w)\end{aligned}$$

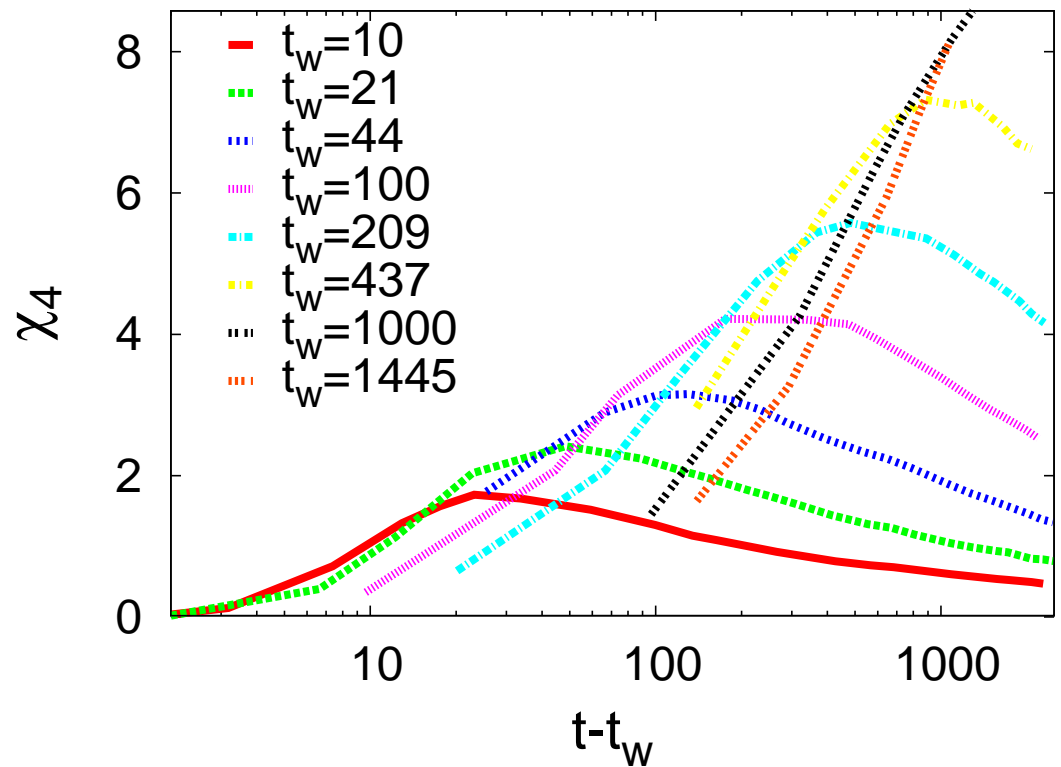
Time evolution of χ_4

Supercooled regime

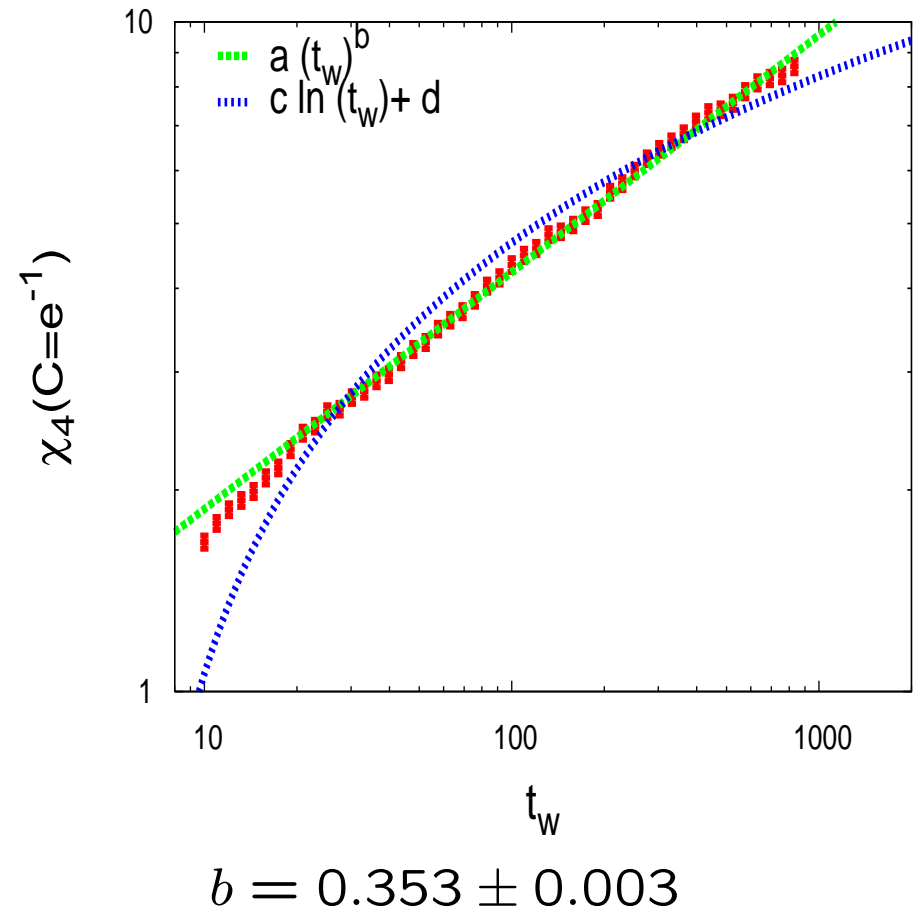
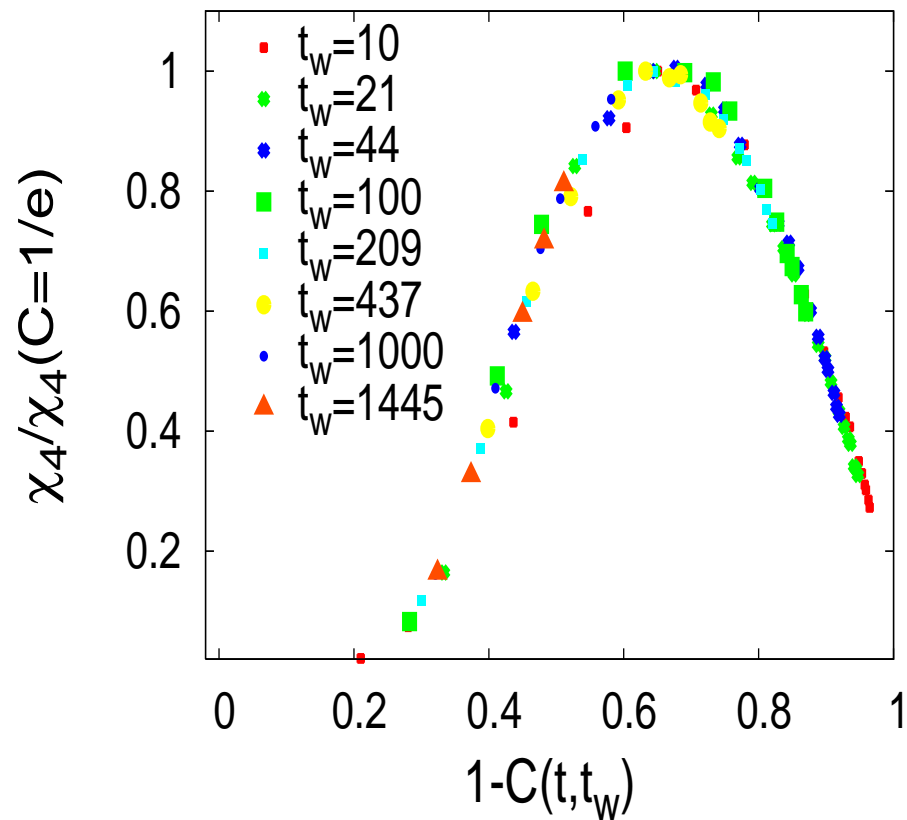
(Starr et al. J. Chem. Phys. 2003)



Aging regime



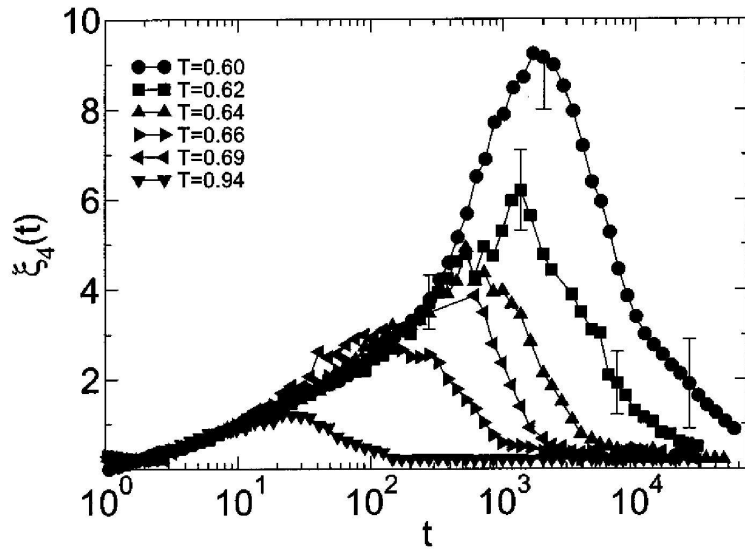
Scaling of χ_4



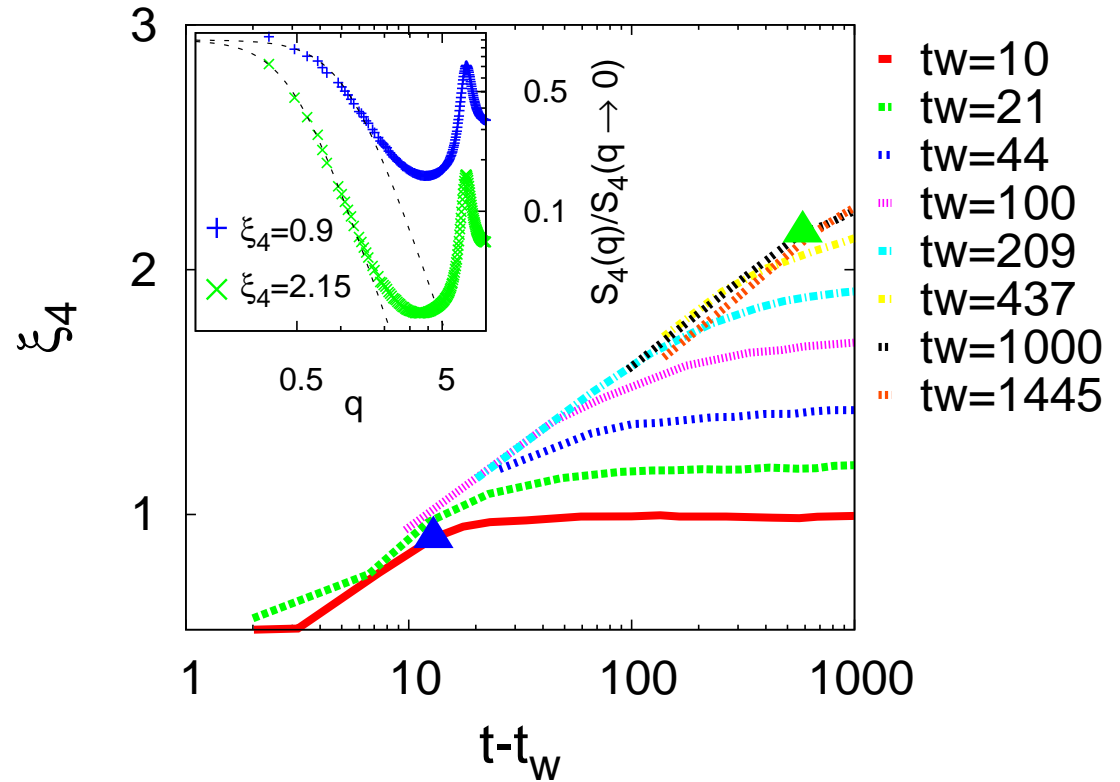
Time evolution of ξ_4

Supercooled regime

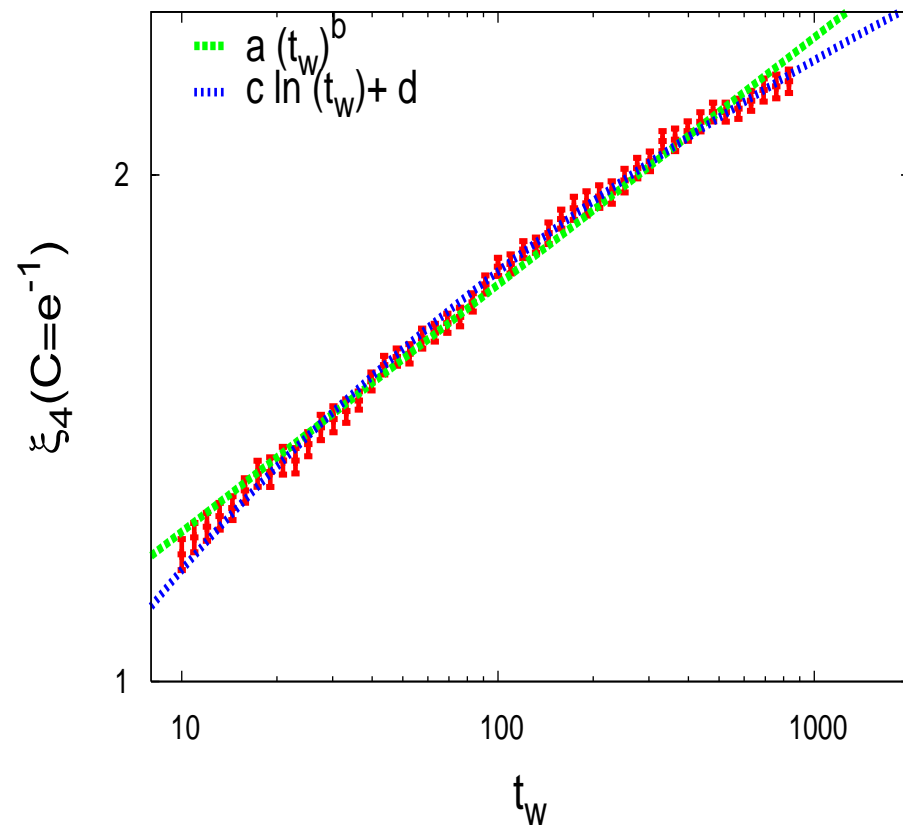
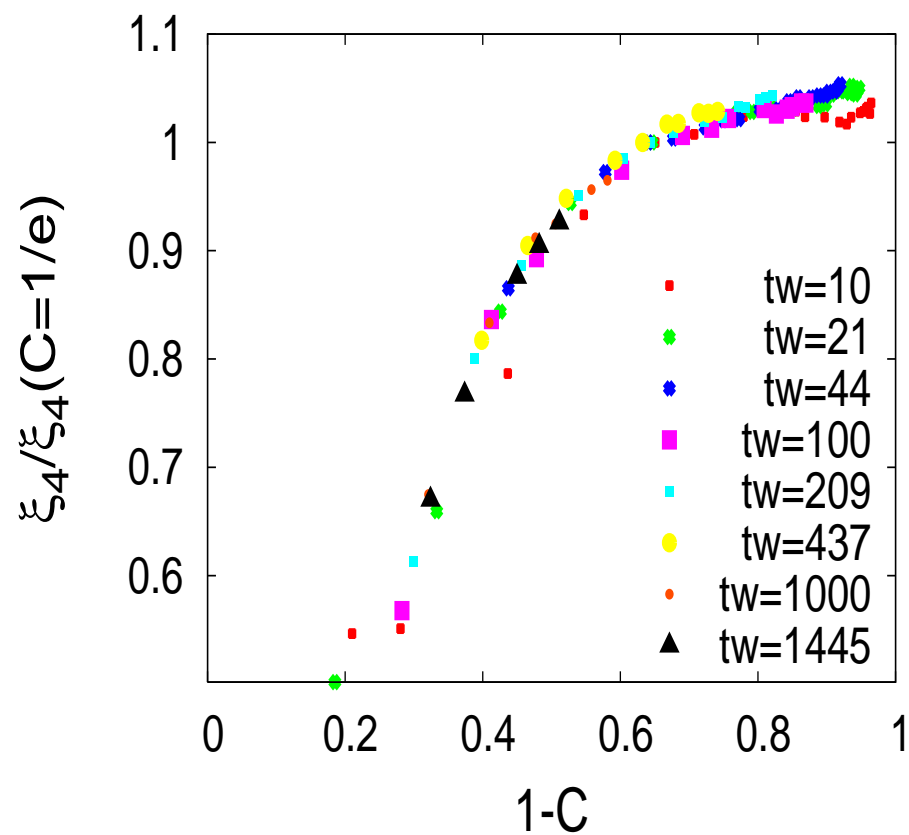
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Aging regime

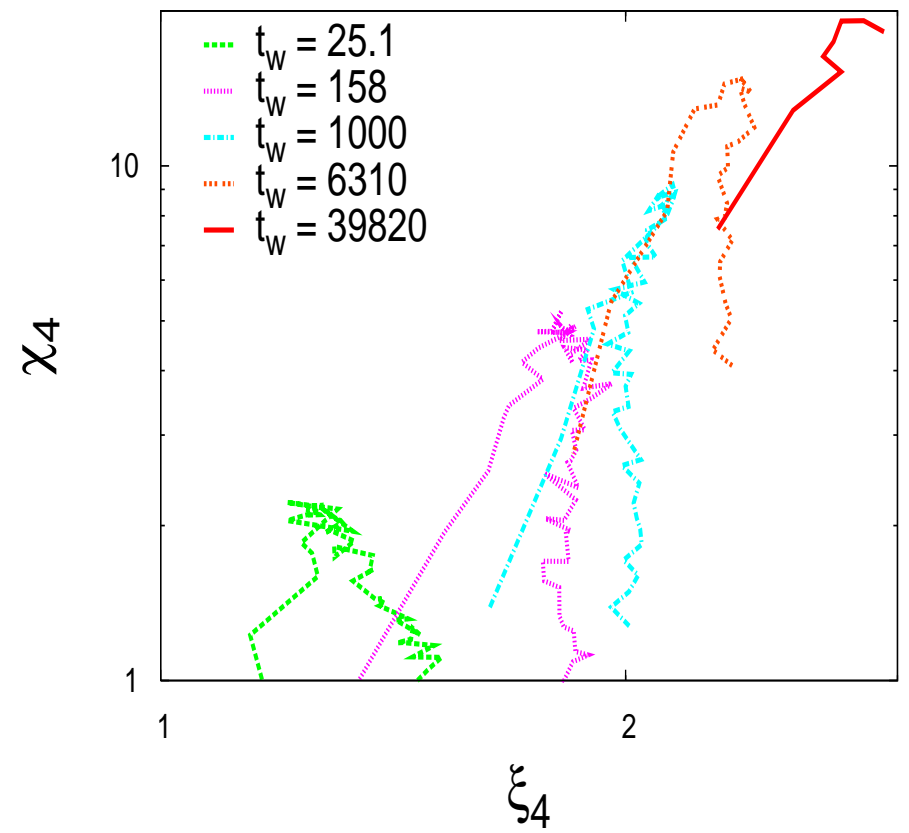
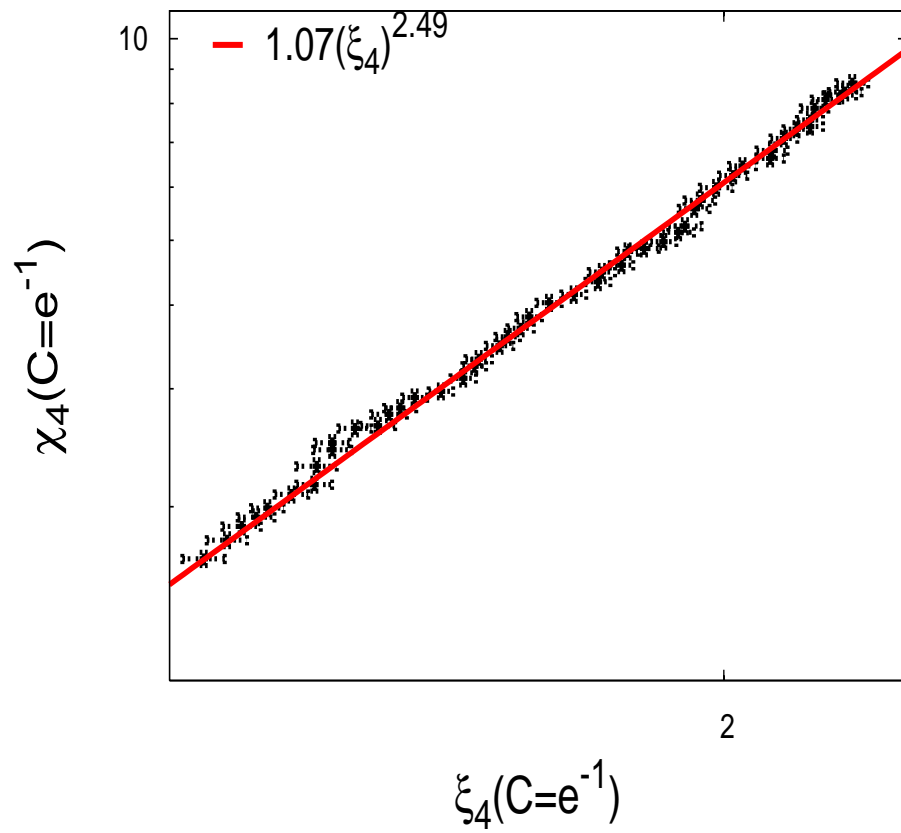


Scaling of ξ_4



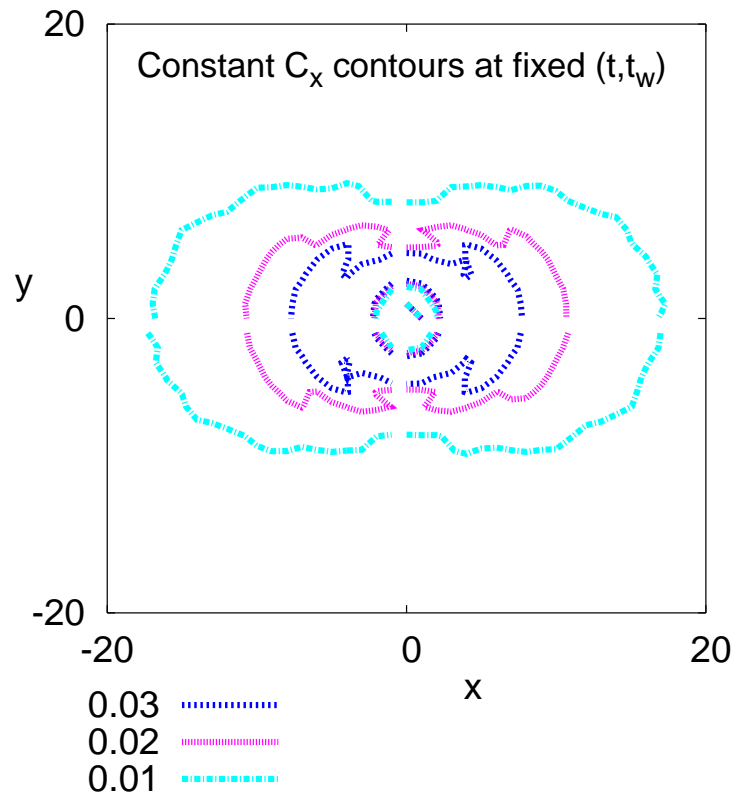
$$b = 0.146 \pm 0.001$$

χ_4 vs. ξ_4

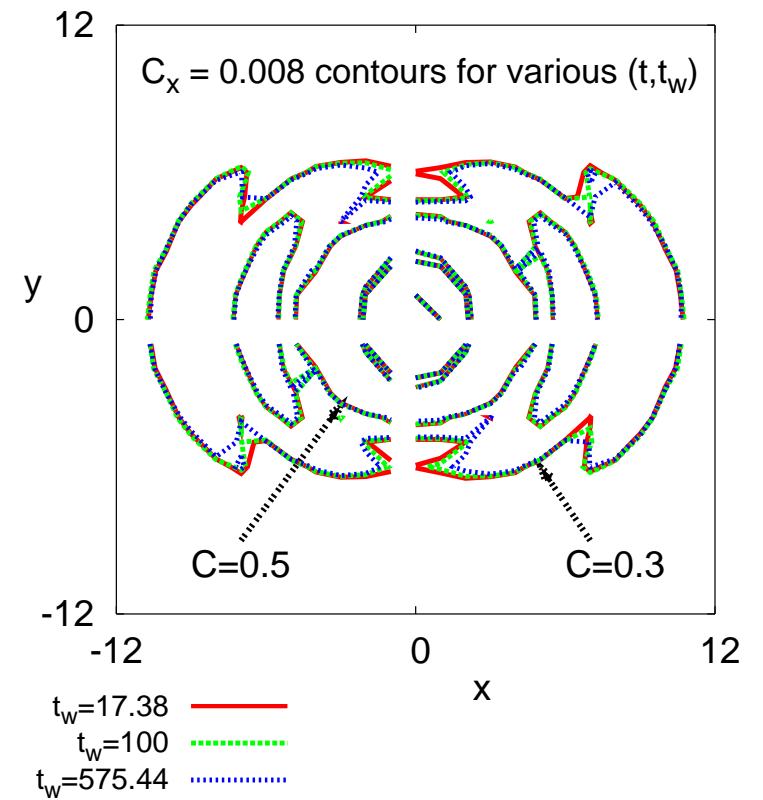


Anisotropy

$$C_x(\mathbf{R}, t, t_w) \equiv \langle \delta x(\mathbf{R}, t, t_w) \delta x(\mathbf{0}, t, t_w) \rangle_c$$



$$t_w = 30.2, t = 2511.88$$



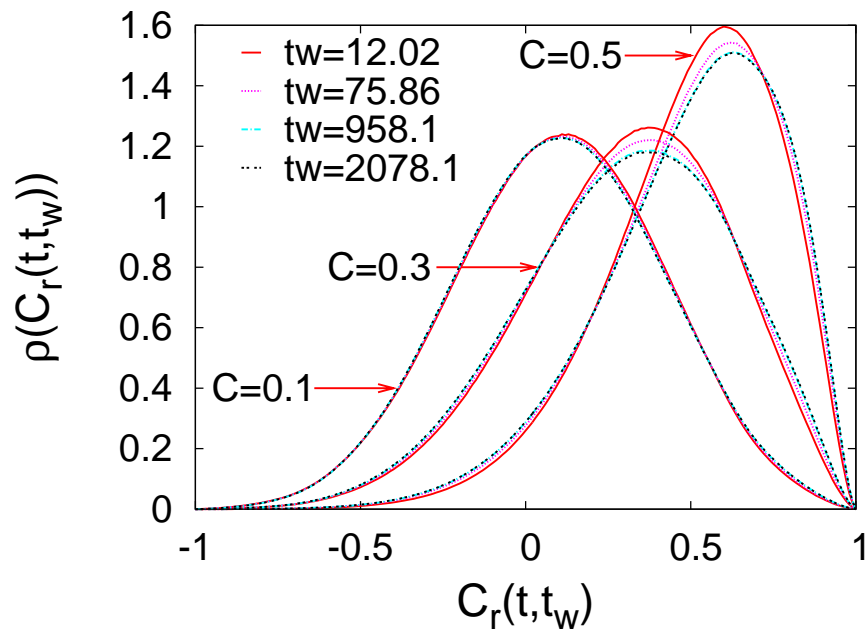
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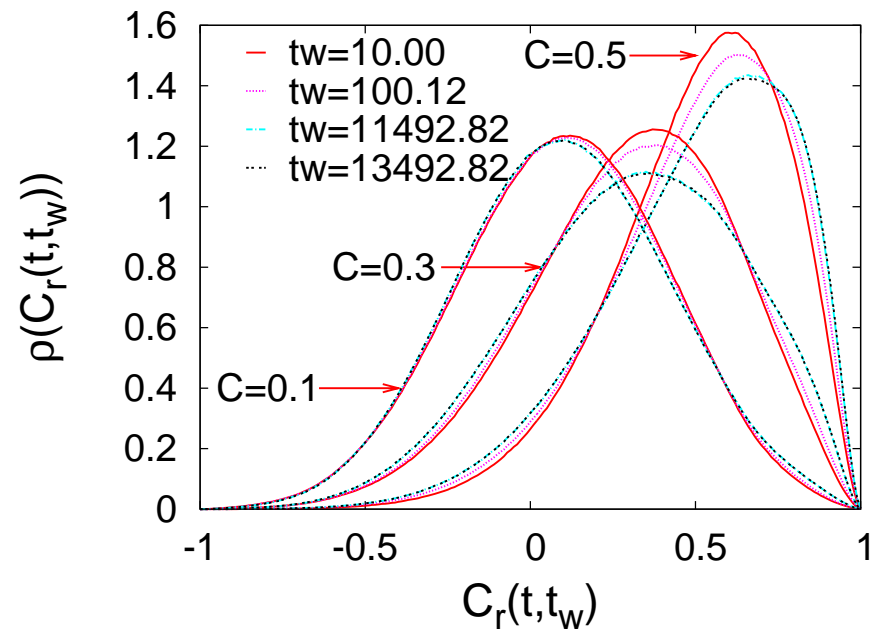
Fluctuations: crossover from aging to equilibrium

WCA potential (repulsive only)

$T = 0.4$



$T = 0.34$

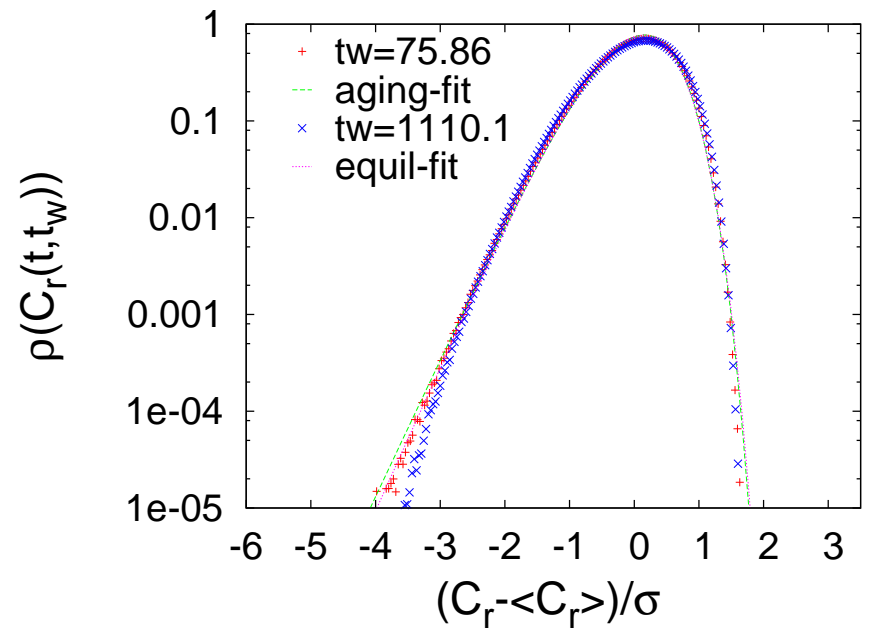
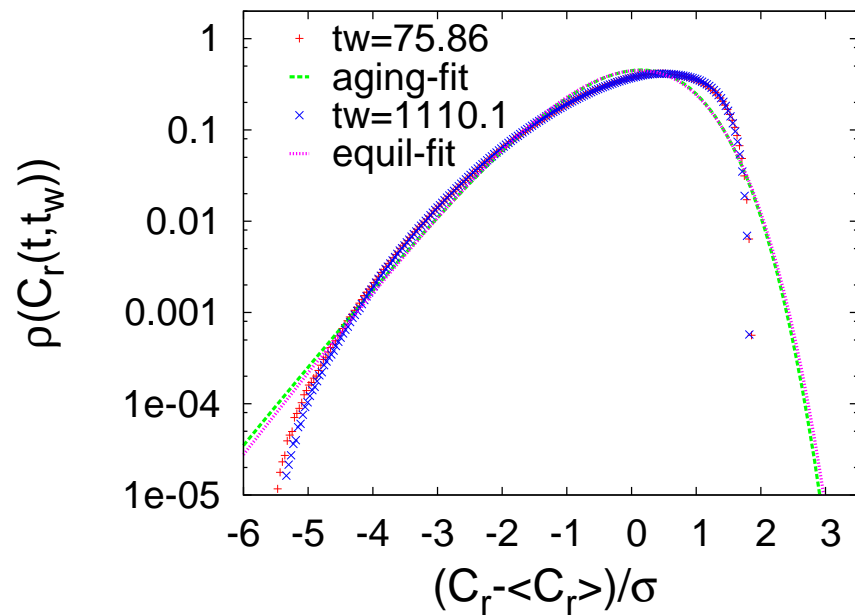


Fluctuations: crossover from aging to equilibrium

WCA potential (repulsive only)

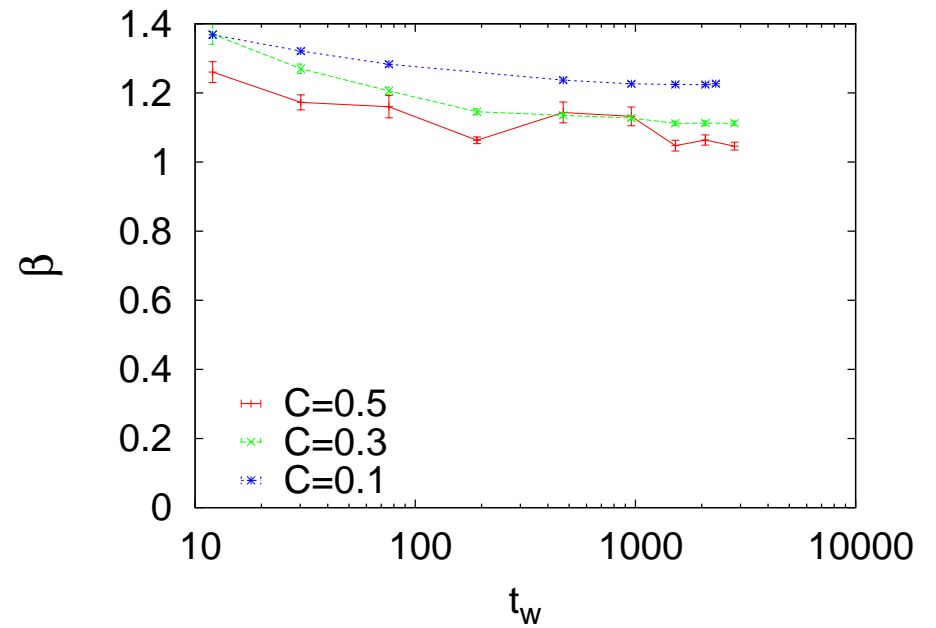
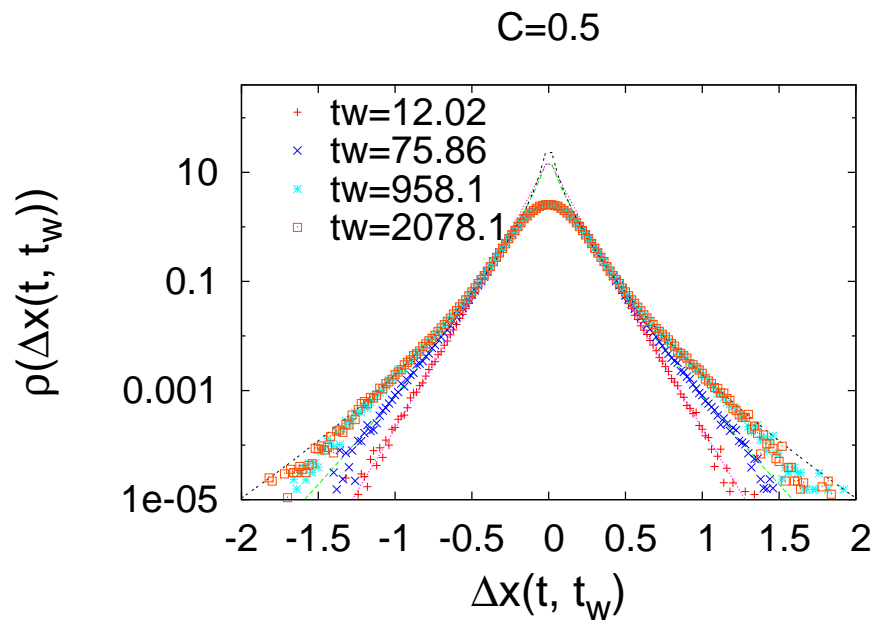
coarse graining: 6.6 particles

coarse graining: 30.5 particles



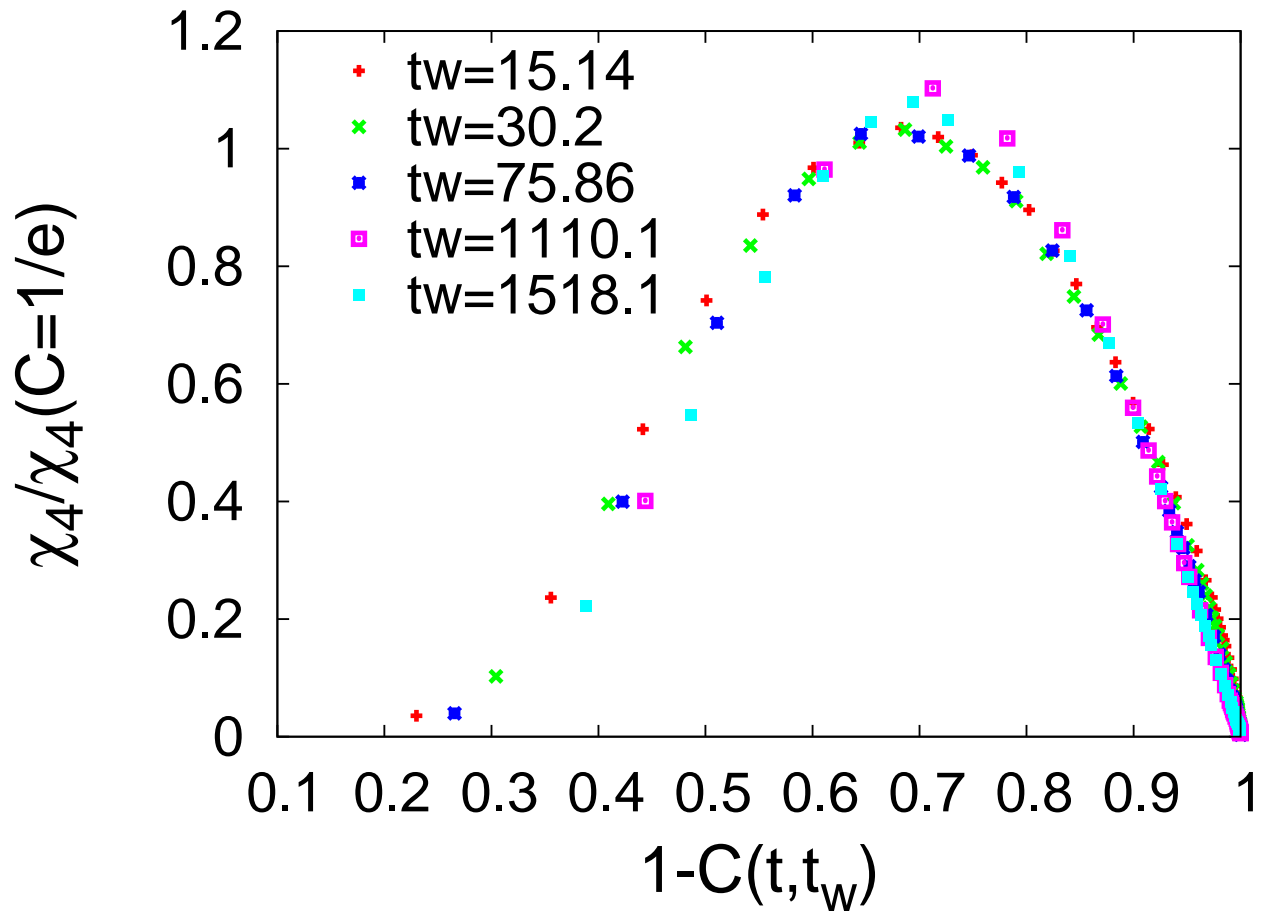
Fluctuations: crossover from aging to equilibrium

WCA potential (repulsive only)



Fluctuations: crossover from aging to equilibrium

WCA potential (repulsive only)



Summary

- Aging in a binary LJ: Probability distributions of local two-time quantities like C_r and Δx show approximate collapse at fixed $C_{\text{global}}(t, t_w)$. Slow drift of distributions with t_w , no timescale observed. Tails of $\rho(\Delta x)$ are nonlinear exponential with exponent $\beta \approx 0.8 - 1.4$, with the lower β corresponding to the longest t_w .
- Aging in a binary LJ: Scaling of 4-point density correlation $\chi_4(t, t_w) \approx \chi_4^0(t_w)\phi(C(t, t_w))$, with $\lim_{C(t, t_w) \rightarrow 0} \phi(C(t, t_w)) = 0$. Scaling of the correlation length $\xi_4(t, t_w) \approx \xi_4^0(t_w)\varphi(C(t, t_w))$, with $\lim_{C(t, t_w) \rightarrow 0} \varphi(C(t, t_w)) = \varphi_0 \neq 0$. Data are consistent with a power law $\chi_4(C = 1/e) \sim (\xi_4(C = 1/e))^b$, however the decay of $\chi_4(t, t_w)$ when $C(t, t_w) \rightarrow 0$ does not correspond to a decay in $\xi_4(t, t_w)$.
- Aging and equilibrium in a binary WCA: One-point distributions seem identical in the aging and equilibrium regimes. (Collapse is better when small coarse graining regions are used due to correlation length effects). The relationship between the rescaled χ_4 and $C(t, t_w)$ is also the same in the aging and equilibrium regimes.

Determination of ξ_4

Fit $S_4(q, t, t_w)$ at small q using the form: $S_4(q, t, t_w) = \frac{a}{1+(\xi_4 q)^\gamma} + b$.

